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# Aerodynamics of Centrifugal Turbine Cascades

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FLUID-DYNAMICS  
OF  
TURBOMACHINES



Dipartimento di Energia

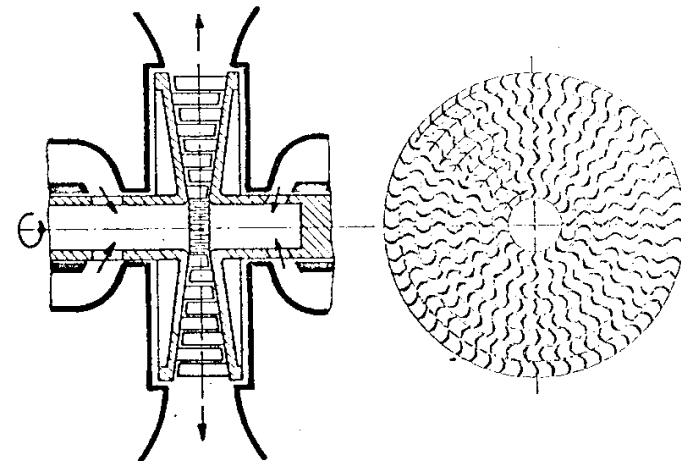
POLITECNICO DI MILANO

- High volumetric expansion ratios → large passage area ratio
- Small enthalpy drops → low number of stages (one-two)
- Organic fluid complexity → low speed of sound

→ highly supersonic axial or centripetal turbines

Interesting alternative: **multistage centrifugal turbine (Exergy configuration)**

- Multistage arrangement in compact configuration
- Intrinsic streamwise increase of cross section
- Novel blade design features for centrifugal set-up



- Preliminary design of a multistage centrifugal turbine
- Aerodynamic design of centrifugal turbine blades
- Three-dimensional aerodynamics of centrifugal stators
- Inertial effects in centrifugal rotors

# Preliminary design of a siloxane MDM turbine

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Pini et al., JEGTP 2013 – ORC Special Issue

## Target conditions

1. Power: 1 MW
2. Flow rate: 22 kg/s
3. Expansion ratio: 60

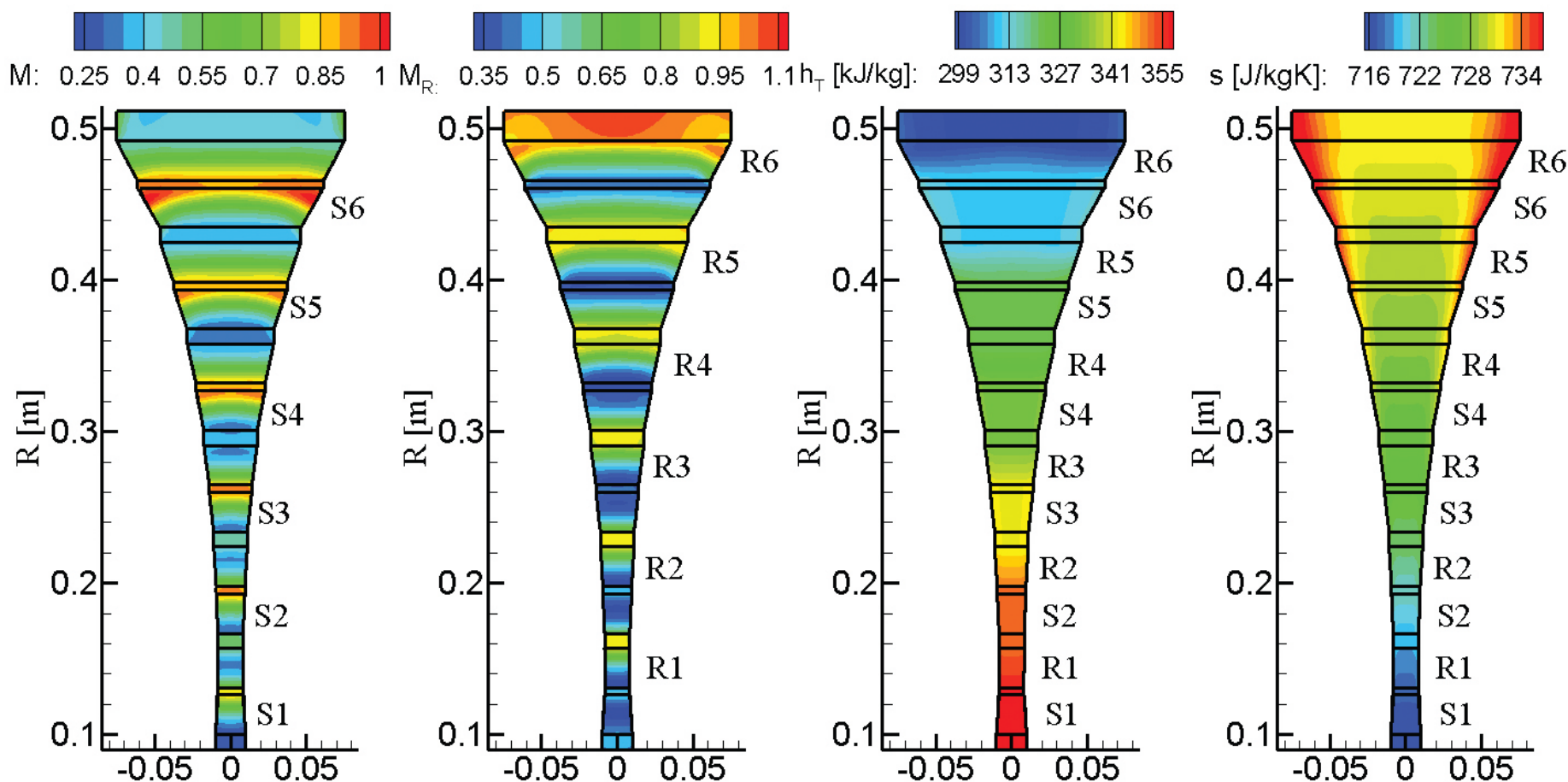
## Stage design data

1.  $M_{\text{MAX}} = 1.0$
2.  $\chi = 0.5$
3.  $\text{Flaring}_{\text{MAX}} = 30^\circ$

## Results

1. N stages = 6
2.  $D_{\text{OUT}} = 1 \text{ m}$
3.  $\eta_{\text{TT}} = 87 \%$

Throughflow results  
confirm expectations:  
✓ Transonic machine  
✓ No choking in design  
✓ High performance

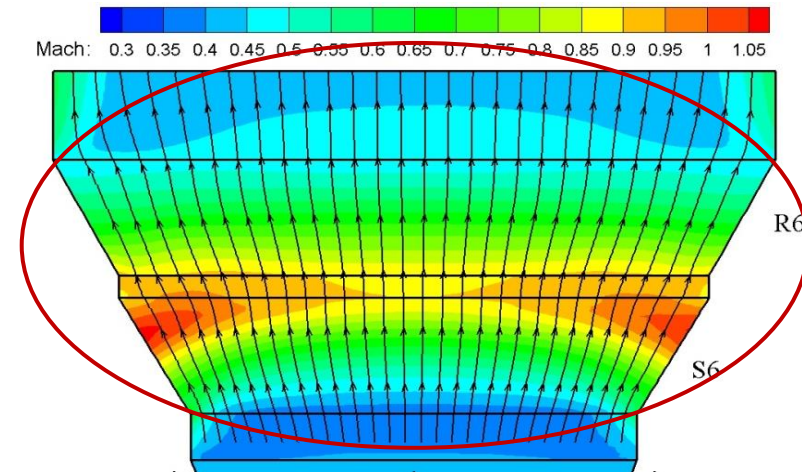


Preliminary design suggests relevant features of centrifugal turbines  
but  
performance estimates based on correlations  
and  
lack of knowledge in open literature about centrifugal cascades

**Investigations on aerodynamics of centrifugal turbine cascades required**  
to  
provide design indications  
investigate specific flow features  
evaluate the reliability of classical correlations (for axial machines)

**Stator** and **rotor** of the **sixth stage** computed in stand-alone configuration

- Fully-3D / quasi-3D steady flow model
- Hexahedral grids with 1.5 / 0.1 Mcells
- Solver: Finite Volume ANSYS-CFX, with:
  - HR methods for inviscid fluxes
  - centred scheme for diffusive terms
- Turbulence model: k- $\omega$  SST with near-wall boundary layer solution (wall  $y^+ \sim 0.3$ )
- Boundary conditions
  - Total quantities, flow angles and turbulence properties imposed at the inlet
  - Static pressure assigned at the exit (iterations due to the vaneless diffusion)
- CFD model validated against experiments (Persico et al., 2012, ASME J. Turbomach.)



- Siloxane MDM thermo-physical properties - estimated using FluidProp<sup>©</sup> :

$$Z_{\text{IN}} = 0.986 \quad Z_{\text{OUT}} = 0.995$$

- Preliminary trials performed with Look-Up-Table approach
- Tests performed with PIG model, calibrated on mean properties.
- Pressure field comparison shows negligible real gas effects

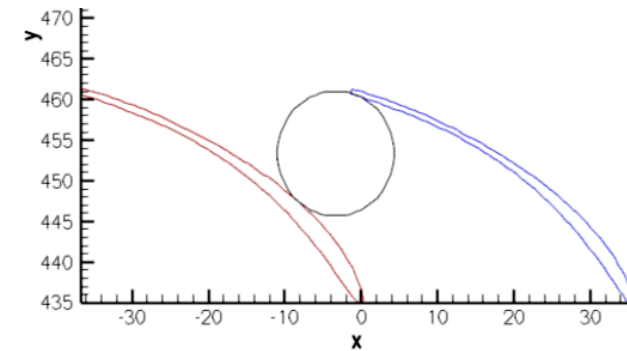
→ **PIG** model used for the calculations

- Preliminary design of a multistage centrifugal turbine
- **Aerodynamic design of centrifugal turbine blades**
- Three-dimensional aerodynamics of centrifugal stators
- Inertial effects in centrifugal rotors



Blade row	$\alpha_{IN} / \beta_{IN} [^\circ]$	$\alpha_{OUT} / \beta_{OUT} [^\circ]$	$M_{OUT}$	$\sigma_b = b/s$ (zweifel)
Sixth stator	$25^\circ$	66.2	0.93	0.75
Sixth rotor	$-36^\circ$	-66.2	0.99	0.65

- No radial equilibrium in spanwise direction  $\rightarrow$  spanwise design not required
- Blade angle definition:
  - . null incidence angle imposed in design condition
  - . deviation estimated via Ainley-Mathieson corr:  
 $\rightarrow$  Gauging  $o/s = f(\alpha_{OUT} \text{ (or } \beta_{OUT}) - dev)$
- Blade construction approach:
  - . mean line assigned
  - . combined with thickness to define SS and PS
- Conformal mapping of the blade sides to conserve the geometric blade angles (not flow!)

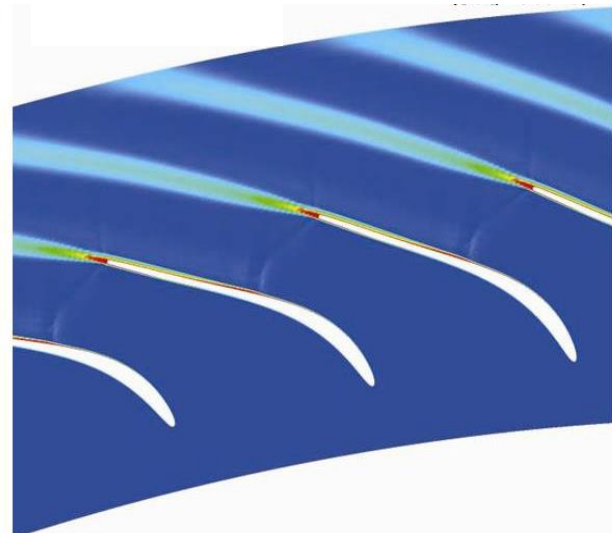
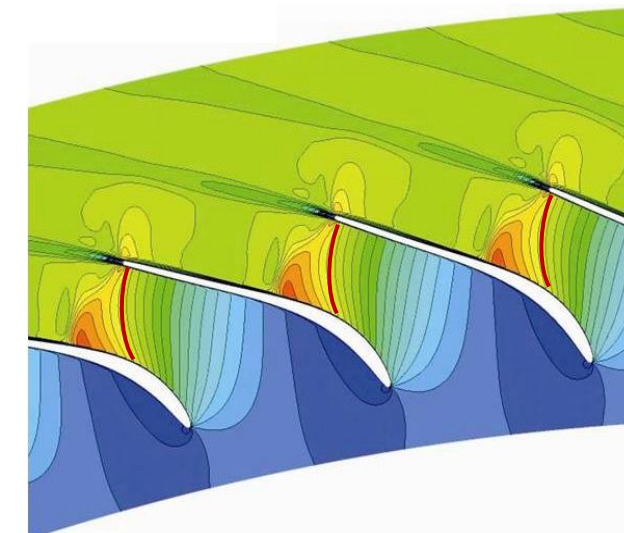
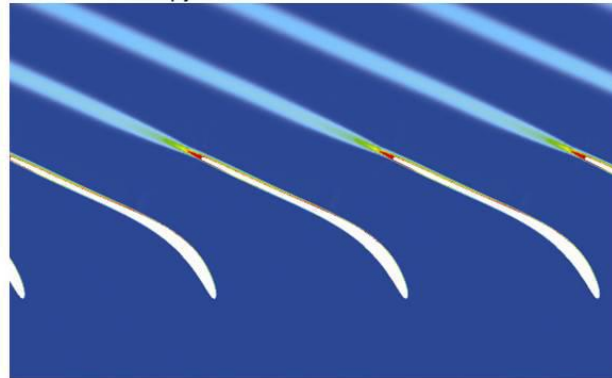
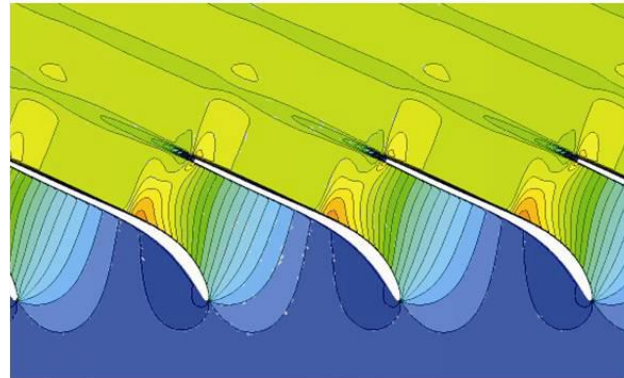
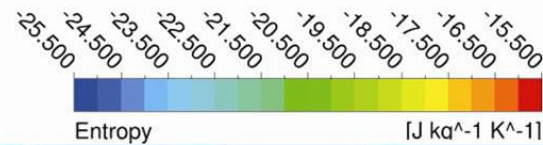
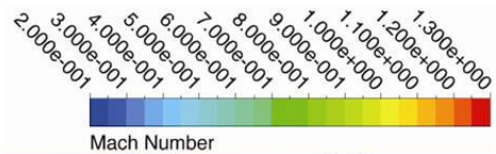


$$r_p = r_{in} \left( e^{\frac{q}{b}(x_p - x_{ref})} \right)$$

$$\theta_p = \frac{q}{b_{ax}} (y_p - y_{ref})$$

# Front-loaded vs aft-loaded profiles

## Front loaded blade aerodynamics



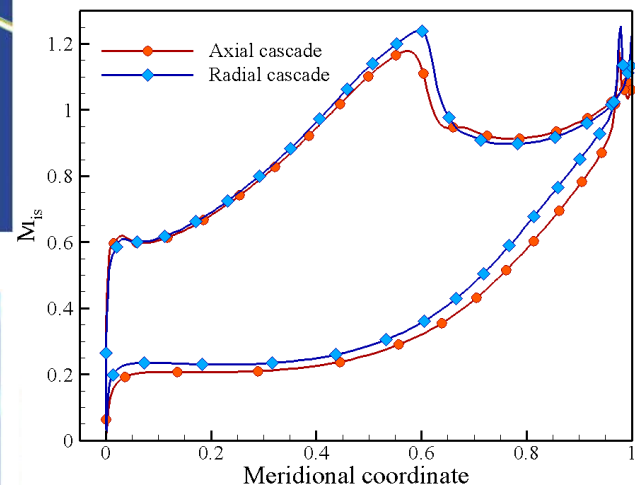
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Smooth flow in axial case

Sonic throat **within** the bladed channel in centrifugal case

→ Straight rear part divergent in centrifugal case!

Choked-flow, stronger shock



→ Higher losses

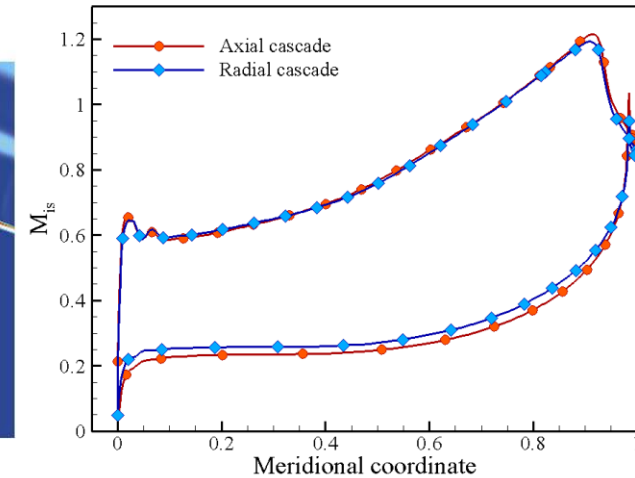
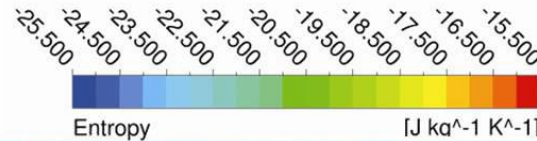
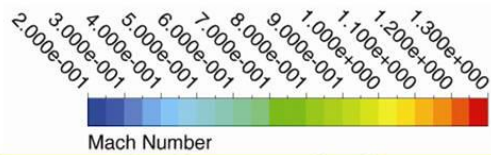
Configuration	$\delta$	$\zeta$	$\zeta_{mix}$
<i>Correlations</i>	0.43°	2.74%	2.74%
<i>Axial</i>	0.45°	3.35%	3.84%
<i>Centrifugal</i>	0.54°	4.96%	4.99%

# Front-loaded vs aft-loaded profiles

## Aft-loaded profile: Elliptic Arc Mean Line blade

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Smooth flow in both cases  
Almost identical expansion process in axial/radial config.



Same strength of SS shock

→ Similar performance

→ Reliability of A-M dev corr

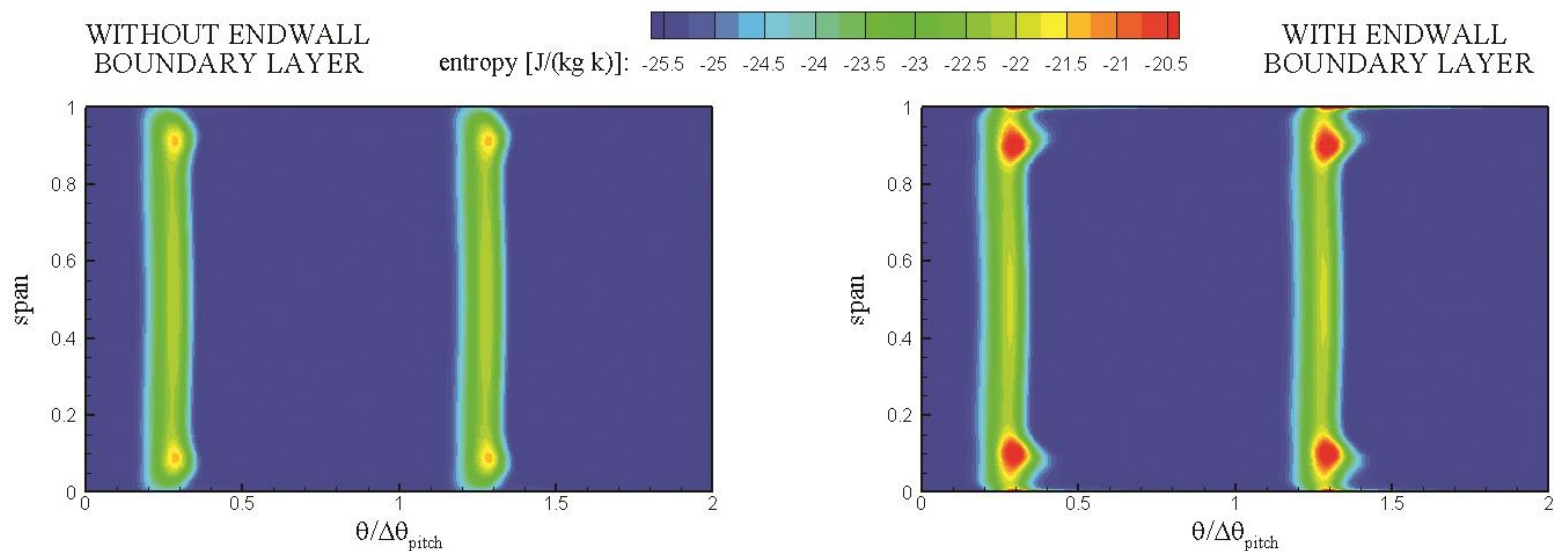
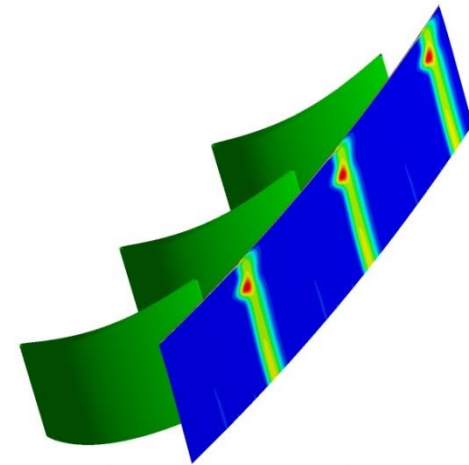
Configuration	$\delta$	$\zeta$	$\zeta_{mix}$
<i>Correlations</i>	-1.9°	2.74%	2.74%
<i>Axial</i>	-1.7°	3.53%	4.01%
<i>Centrifugal</i>	-1.9°	3.00%	3.27%

- Preliminary design of a multistage centrifugal turbine
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## Three-dimensional flow configuration

Endwall boundary layer treatment:

- (a) Endwall slip condition  $\rightarrow$  flaring effects isolated
- (b) Endwall No-slip condition  $\rightarrow$  secondary flows included

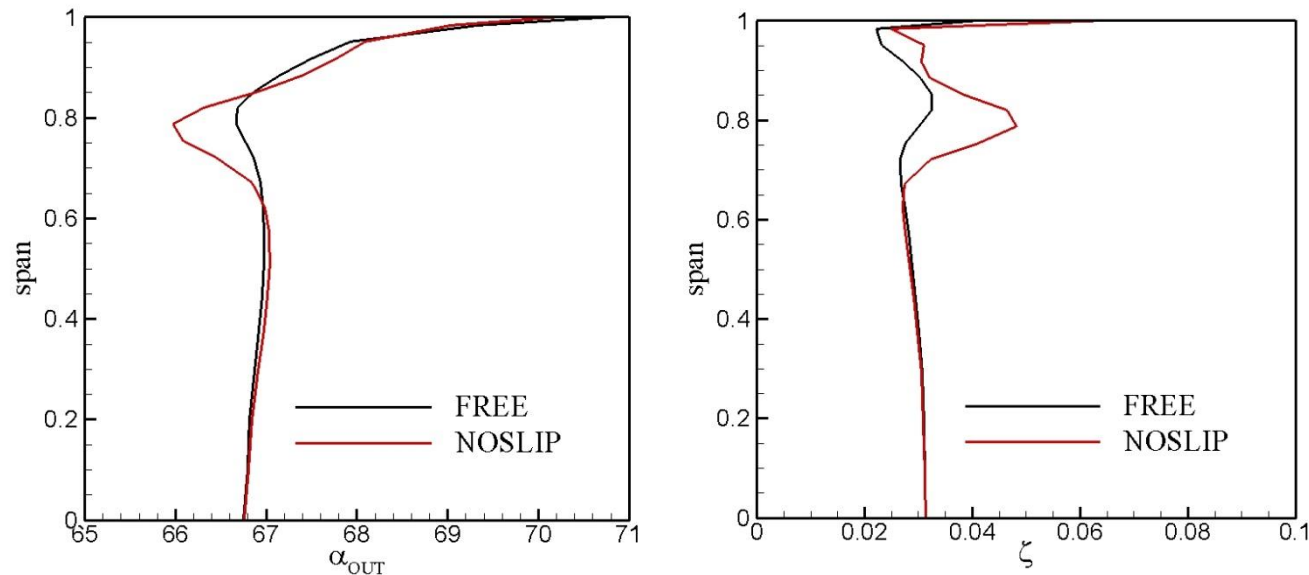


- (a): wake endwall gradient due to flaring  $\rightarrow$  spanwise variation of blade loading
- (b): distinct loss cores due to secondary vortices  $\rightarrow$  no rad. eq., spanwise symmetry



## Spanwise profiles and performance

- Spanwise gradients without endwall BL due to flaring  
→ meridional velocity ↓, flow angle ↑ (1° in mean flow angle)
- Larger effects in case of secondary vortices: over/under-turning, loss peaks



Cascade	C-C corr (3D)	CFD-quasi 3D	CFD-3D-slip	CFD-3D-noslip
$\zeta_{mix}$	7.3	3.27	3.7	4.03

**computed overall loss coefficient 40% smaller than correlation prediction**

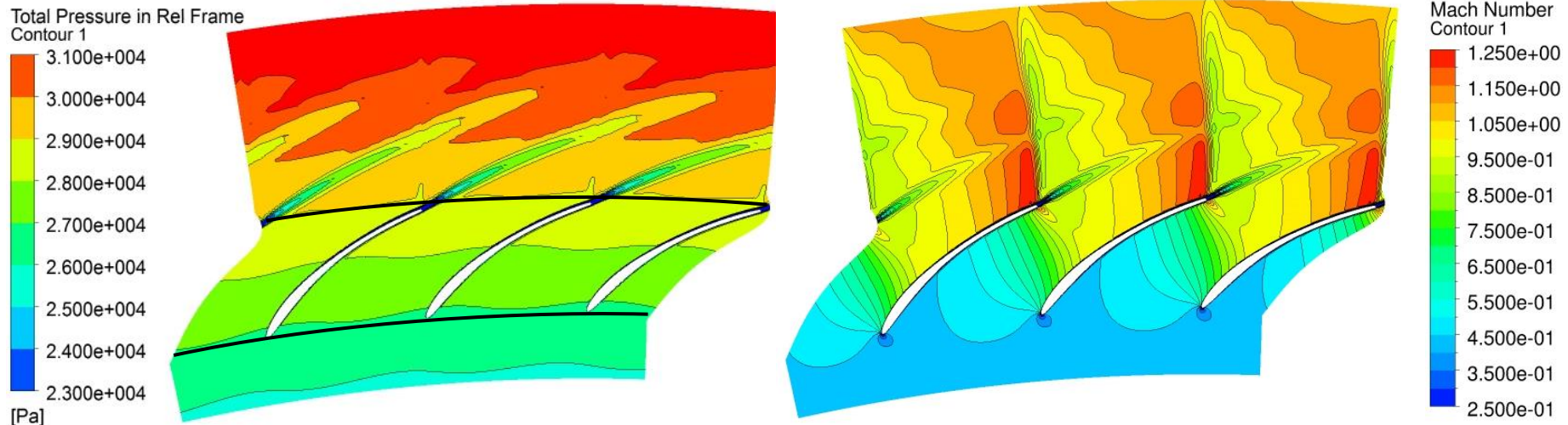
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## Apparent forces features

Coriolis and centrifugal forces  $\rightarrow$  impact on profile aerodynamic design?

Centrifugal force  $\rightarrow T_{TR}, P_{TR}, M_R \uparrow$  in outward direction  $\rightarrow$  strong TE shock

Coriolis force  $\rightarrow$  slip effect on flow angle  $\rightarrow$  more tangential flow expected



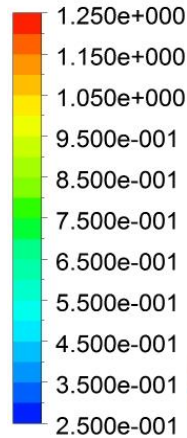
Fixed-rotor calculations assigning relative quantities to highlight inertial effects

Not univocal choice of inlet relative total quantities  $\rightarrow$  both LE & TE considered

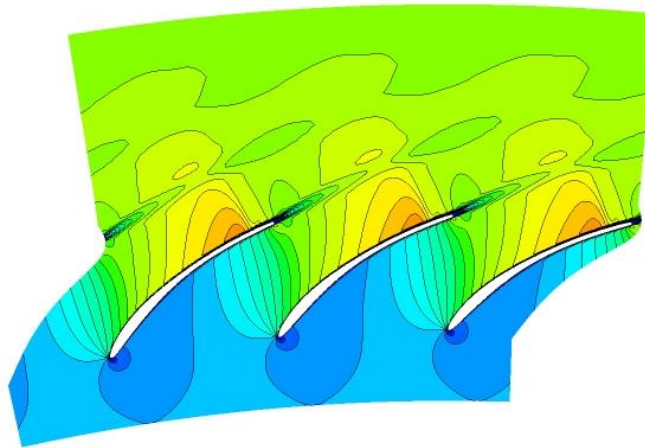


## Impact on aerodynamics & performance

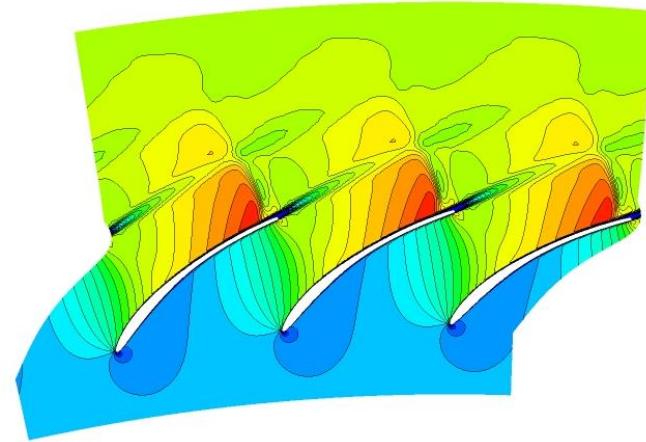
Mach Number  
Contour 1



FIXED  $P_{T,in} = P_{TR,LE}$



FIXED  $P_{T,in} = P_{TR,TE}$

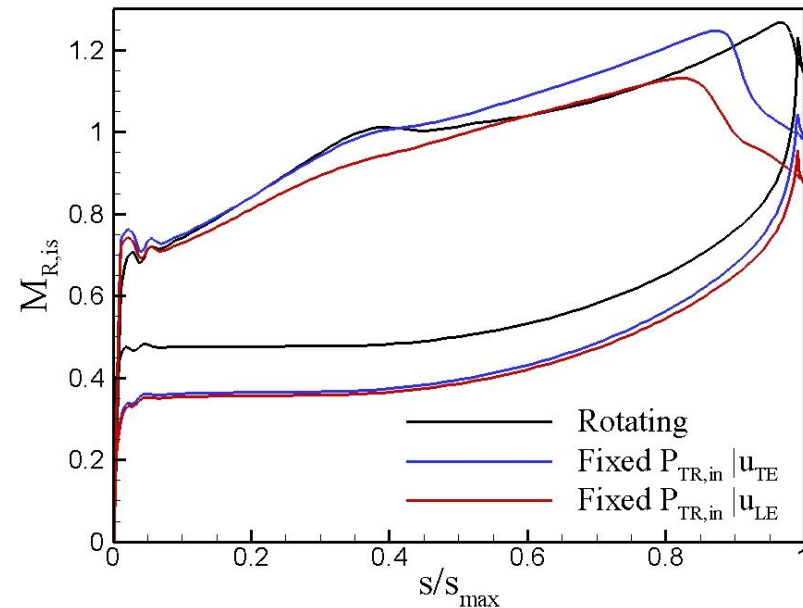


$P_{T,in} = P_{TR,LE} \rightarrow$  no match in  $M_{OUT}$ , no shocks

$P_{T,in} = P_{TR,TE} \rightarrow$  match in  $M_{OUT}$ , different shock

$\rightarrow$  No way to reproduce pressure distribution of rotating blade rows with stationary experiments

More tangential flow due to (weak) Coriolis effect



Case	$\alpha_{OUT}$	$M_{OUT}$	$\zeta_{mix}$
Rotating	$-67.6^\circ$	0.985	4.85%
FixedRT <sub>IN</sub>	$-67.1^\circ$	0.920	2.86%
FixedRT <sub>OUT</sub>	$-66.7^\circ$	0.989	3.68%

- Preliminary design **suggests** potential of centrifugal turbine architecture
- Aerodynamic study with high-fidelity CFD **assesses** turbine stage performance
- **Aft-loaded** profiles (such as **EAML**) outperform front loaded ones
- Three dimensional effects are relevant in case of large flaring
- Centrifugal force determines the aerodynamics of centrifugal rotor blade rows
  - stator blade design criteria not entirely extendable to rotor blades
  - stationary experiments of limited validity of rotor blade profiles

**Loss correlations overestimate stage losses in preliminary design**

**→ last stage efficiency rises from 91.7% (preliminary) to 92.3% (H-F CFD)**

**Further step: to apply the design procedure to the first stages**

**→ to test the design strategy for higher radial effects**

**→ to evaluate the improvement in overall turbine efficiency**